Control of Industrial and Mobile Robots

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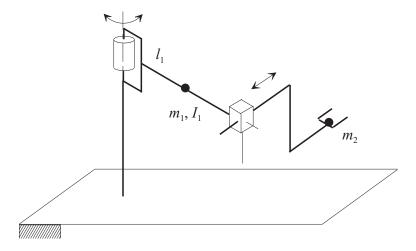
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Warnings

- This file consists of **10** pages (including cover).
- During the exam you are not allowed to exit the room for any other reason than handing your work or withdrawing from the exam.
- You are not allowed to withdraw from the exam during the first 90 minutes.
- During the exam you are not allowed to consult books or any kind of notes.
- You are not allowed to use calculators with graphic display.
- Solutions and answers can be given either in English or in Italian.
- Solutions and answers must be given **exclusively in the reserved space**. Only in the case of corrections, or if the space is not sufficient, use the back of the front cover.
- The clarity and the order of the answers will be considered in the evaluation.
- At the end of the test you have to **hand this file only**. Every other sheet you may hand will not be taken into consideration.

EXERCISE 1

1. Consider the manipulator sketched in the picture, where the mass of the second link is assumed to be concentrated at the end-effector:



Find the expression of the inertia matrix $\mathbf{B}(\mathbf{q})$ of the manipulator.



3. Check that matrix $\mathbf{N}(\mathbf{q}, \dot{\mathbf{q}}) = \dot{\mathbf{B}}(\mathbf{q}) - 2\mathbf{C}(\mathbf{q}, \dot{\mathbf{q}})$ is skew symmetric.

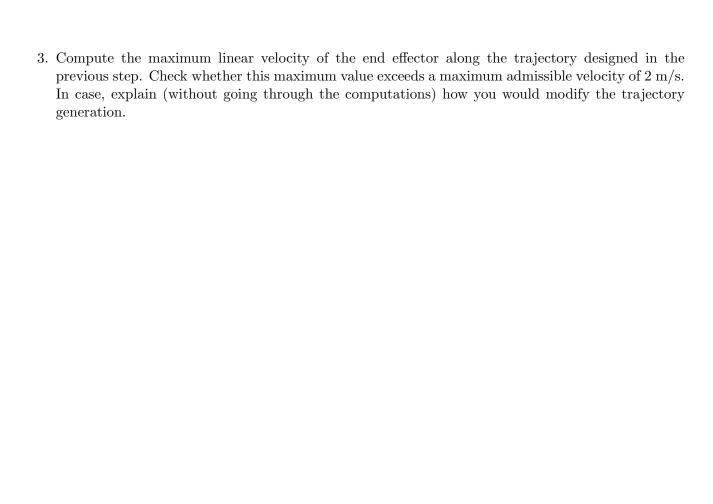
4. Cite one case in robotics where the property that matrix $\mathbf{N}(\mathbf{q}, \dot{\mathbf{q}})$ is skew symmetric is used.

The general expression of the Christoffel symbols is $c_{ijk} = \frac{1}{2} \left(\frac{\partial b_{ij}}{\partial q_k} + \frac{\partial b_{ik}}{\partial q_j} - \frac{\partial b_{jk}}{\partial q_i} \right)$

EXERCISE 2

1. Consider the generation of a position trajectory in the Cartesian space. Select as an initial point $\mathbf{p}_i = \begin{bmatrix} 3 \\ 1 \\ 1 \end{bmatrix}$ and as a final point $\mathbf{p}_f = \begin{bmatrix} 0 \\ 1 \\ 5 \end{bmatrix}$. Write the expression of a segment connecting the initial and the final points, parameterized with the natural coordinate.

2. Assume a travel time T=2s. Design a trajectory, which covers the path determined in the previous step, using a cubic dependence on time.

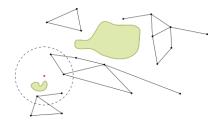


4. Suppose that the manipulator is kinematically redundant for the task of end effector positioning. Write the expression of the inverse kinematics based on the *weighted* pseudo-inverse matrix and explain what is the optimization problem solved with this approach. Also explain what might be the reason to use the weighted pseudo-inverse instead of the standard pseudo-inverse matrix.

EXERCISE 3

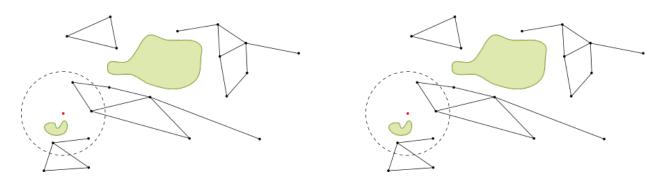
(E	ERCISE 3
1.	Write and explain the pseudocode of the algorithm to construct the probabilistic roadmap used by PRM.
2.	Explain how the previous algorithm has to be modified in order to obtain sPRM and PRM* al-
	gorithms.

3. After the execution of some iterations of PRM algorithm we have the situation depicted below



where the black dots are the nodes sampled in previous iterations, the red dot is the node sampled in the actual iteration, the green blobs are obstacles and the black dashed circle is the neighbourhood considered to defined the Near set.

Draw in the left picture the result of an iteration of PRM and in the right picture the result of an iteration of sPRM.



4. What is the main difference between PRM (or sPRM or PRM*) and RRT (or RRT*)?

EX

XF	CRCISE 4
1.	What is the canonical simplified model for nonholonomic mobile robots? Why is it important in the context of designing a controller for a nonholonomic robot?
2	Show how the unicycle, differential drive, and rear-wheel drive bicycle kinematic models can be made equivalent to the canonical model.

